

## REFERENCES

Of the following references only those cited in the text were used directly. The rest are included for the convenience of those who wish to read further concerning algebraic flows in the plane. The books by Sansone and Conti, Nemytskii and Stepanov, and Bhatia and Szegö contain a large number of further references.

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